

# CLIPPR: Maximally Informative CLIPped PProjections with Bounding Regions

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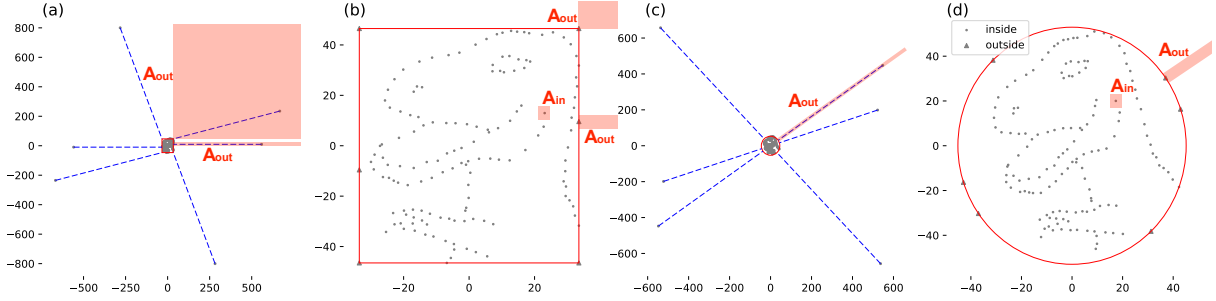


Figure 1: CLIPPR is an algorithm for generating maximally informative clipped projections with bounding regions. The projection shown in (a) features a dense core of occluded points as well as a set of outliers. By finding an appropriate bounding box, a *clipped projection* is obtained in (b). In the clipped projections, points outside the bounding region are shown with triangular markers on the boundary. CLIPPR can also produce elliptical bounding regions. The data consists of six artificial outliers plus Alberto Cairo’s figure: <http://www.thefunctionalart.com/2016/08/download-datasaurus-never-trust-summary.html>.

## ABSTRACT

While there are various established methods used for projection, many projections fail to capture phenomena at different scales, due to occlusion or overplotting. A trade-off emerges between showing small and large-scale structure. In this work, we present an algorithm that parameterizes this tradeoff to calculate multiple projections that vary by the scale of the highlighted structure. By jointly optimizing both the *information theoretic content* of the projection and the clipped bounding region of the resulting view, we can empirically find relevant structure to show to a user. We describe how this method would be useful in a visual analytics system for providing a *grand tour* for both low- and high-dimensional datasets. By exposing a simple resolution parameter to the user, the user is able to guide their own path through their data, enabling them to glean multiple levels of insight in a way that other static projection techniques could not allow.

**Index Terms:** Human-centered computing—Visualization—Visualization techniques; Computing methodologies—Machine Learning—Dimensionality reduction and manifold learning;

## 1 INTRODUCTION

Imagine a scenario where an analyst is examining a new dataset of real numbers. The analyst plots the dataset as a 2-dimensional scatterplot and sees a small blob of overplotted points and a few outliers such as the image shown in Figure 1(a). The analyst is unable to see the clear structure seen in the zoomed in view in Figure 1(b).

The need to show all data points, including the outliers, results in overplotting of many of the data points. Due to the limits of human perception, even if no two data points in Figure 1(a) appear on the same pixel (possibly because of an ultra-high resolution display), the result still appears to be cluttered. The user would not be able to discern the underlying pattern as easily in Figure 1(a) as if the data is presented in a “zoomed in” way as in Figure 1(b).

In this work, we propose a technique to automatically identify *clipped projections* of high-dimensional data in a 2-dimensional subspace. Our technique, CLIPPR, is based on maximization of the information content within the clipped projections. The optimization exposes a *resolution parameter* that can be set by a user or a visualization designer to control the scale of visual phenomena found in data.

## 2 RELATED WORK

Most projection techniques optimize a particular metric that is defined over every possible projection. Principal Component Analysis [3] optimizes variance captured in each dimension. If we ignore clipping (or if the clipped projection includes all points inside the bounding box), our technique can be made equivalent to PCA [4]. Multidimensional Scaling [5] optimizes the ratio of differences between data space and projected space. More similar to CLIPPR are Stochastic Neighbor Embedding (SNE) techniques [2, 6], in which the location of a projected point is expressed as a random variable, and the dissimilarity (KL-divergence) of the joint distributions (over the random variables) between data space and projected space is minimized. Note, however, that CLIPPR results in *linear* projections, while SNE projections are non-linear and thus distort distances and shapes in data.

## 3 METHOD

Any projection of data requires a metric that determines how to rank potential projections [1]. For example, PCA maximizes the variance found in the first two dimensions with the assumption that maximum variance in the data means showing the most information to the user that is possible to see in two dimensions. However, in many cases, the variance in the dataset may not be particularly

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interesting. Consider outliers as in Figure 1. They contribute largely to the variance of the dataset, but they do not add to the user’s understanding of the relevant structure in the data (i.e., the dinosaur in the center).

Instead, we propose a metric that rewards projections that are result in many points being spread out and discernible. We can optimize the Information Content (IC) of a clipped projection, where IC is defined as a function of the *visible* points inside a bounding box, with respect to a Gaussian background distribution.

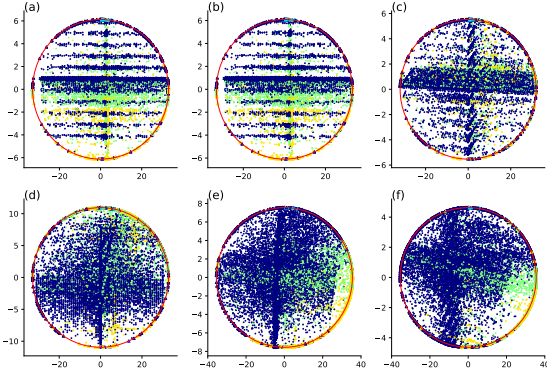


Figure 2: Grand tour on UCI shuttle dataset. (a) - (f) show increasing values of  $f$  resolution parameter. Points are colored by their class label. By varying the  $f$  parameter, different relationships between classes emerge.

Let  $s$  be the bounding box parameters and  $f$  be a resolution parameter controlling how far away two points need to be in order to be *discernible*. We will denote the projections of a data set  $\hat{\mathbf{X}}$  onto the column vectors of  $\mathbf{W}$  as  $\hat{\Pi}_{\mathbf{W}} \in \mathbb{R}^{n \times k}$ , and  $\mathbf{A}(\hat{\Pi}_{\mathbf{W}}, f, s)$  be the union of discernible regions of points in the projection. We can define the probability that a weight matrix  $\mathbf{W}$  generated a clipped projection.

$$\begin{aligned} \Pr(\hat{\Pi}_{\mathbf{W}} \in \mathbf{A}(\hat{\Pi}_{\mathbf{W}}, f, s)) &= \int_{\mathbf{A}(\hat{\Pi}_{\mathbf{W}}, f, s)} p_{\Pi_{\mathbf{W}}}(\Pi_{\mathbf{W}}) d\Pi_{\mathbf{W}} \\ &= \prod_{i=1,2,\dots,n} \left[ \int_{\mathbf{z}_i \in \mathbf{A}(\hat{\mathbf{z}}_i, f, s)} p_{\Pi_{\mathbf{W}}}(\mathbf{z}_i) d\mathbf{z}_i \right]. \end{aligned} \quad (1)$$

The goal of finding the most informative clipped projection can be formalized as an optimization problem:

$$\begin{aligned} \text{IC}(\mathbf{W}, \hat{\Pi}_{\mathbf{W}}, s) &= -\log \Pr(\hat{\Pi}_{\mathbf{W}} \in \mathbf{A}(\hat{\Pi}_{\mathbf{W}}, f, s)). \\ \underset{\mathbf{W}, s}{\operatorname{argmax}} \quad &\text{IC}(\mathbf{W}, \hat{\Pi}_{\mathbf{W}}, s), \\ \text{s.t.} \quad &\mathbf{W}'\mathbf{W} = \mathbf{I}, \quad s > 0. \end{aligned}$$

## 4 EXPERIMENTS

The experiments are conducted using a Python implementation of CLIPPR, which, along with the datasets used, have been made publicly available for the purpose of reproducibility.<sup>1</sup>

<sup>1</sup>Implementation of CLIPPR and the datasets can be found online at <https://bitbucket.org/ghentdatascience/clippr>, and demo is at <https://www.eecs.tufts.edu/~dcashm01/clippr>

For brevity, we provide information on two experiments. First, we demonstrate two types of bounding regions supported by CLIPPR, rectangles and ellipses. These are demonstrated on a synthetic dataset, described in Fig. 1.

We also experimented with varying the resolution parameter to uncover more than one scale of phenomenon in multiple projections. To explore this, we ran CLIPPR on a real dataset at six different settings of the resolution parameter, visible in Fig. 3. The UCI Shuttle dataset<sup>2</sup> consists of 14,500 testing examples from a shuttle flight. Initially, we see that data items of the blue class seem to differ by regular intervals, suggesting that there exists a discrete binning of one variable in the dataset that varies across the blue class. As the  $f$  parameter is swept higher, the blue points cluster into a single horizontal and single vertical component. The two scales reveal two different structures in the data.

## 5 DISCUSSION

While various projection methods are used to visualize the data, many of them fail to capture phenomena at different scales. Methods like PCA and MDS that optimize for showing the large-scale structure can over-represent outliers, whereas methods like tSNE emphasize the small-scale structure but can present spurious global structures. In this paper, we present CLIPPR, an algorithm that aims to optimize the information content of the visualization, searching for the most informative structure of a given dataset. The experiments also suggests that CLIPPR can be used by visualization designers to carefully craft their own projection.

CLIPPR is not yet efficient enough to provide real-time data exploration. Currently, CLIPPR needs to pre-render a series of projections to provide a grand tour. Improving the scalability of CLIPPR is an important direction for further investigation. Also, optimizing the information content of clipped projections with bounding box that has higher degrees of freedom (e.g., shifting center) is also worth examining.

## ACKNOWLEDGMENTS

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<sup>2</sup>[https://archive.ics.uci.edu/ml/datasets/Statlog+\(Shuttle\)](https://archive.ics.uci.edu/ml/datasets/Statlog+(Shuttle)), ‘shuttle.tst’